AUTOMATIC CLASSIFICATION: NAÏVE BAYES

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R. Basili

(slides borrowed by: H. Schutze)

Università di Roma "Tor Vergata" Email: basili@info.uniroma2.it

Summary

- Probabilistic Algorithms for Automatic Classification (AC)
 - Naive Bayes
 - Two models:
 - Univariate Binomial
 - Multinomial (Class Conditional Unigram Model)
- Parameter estimation & Feature Selection
- Evaluating an AC system

Motivation: Is this spam?

From: "" <takworlld@hotmail.com>

Subject: real estate is the only way... gem oalvgkay

Anyone can buy real estate with no money down

Stop paying rent TODAY!

There is no need to spend hundreds or even thousands for similar courses

I am 22 years old and I have already purchased 6 properties using the methods outlined in this truly INCREDIBLE ebook.

Change your life NOW!

Click Below to order:

http://www.wholesaledaily.com/sales/nmd.htm

Categorization/Classification

• Given:

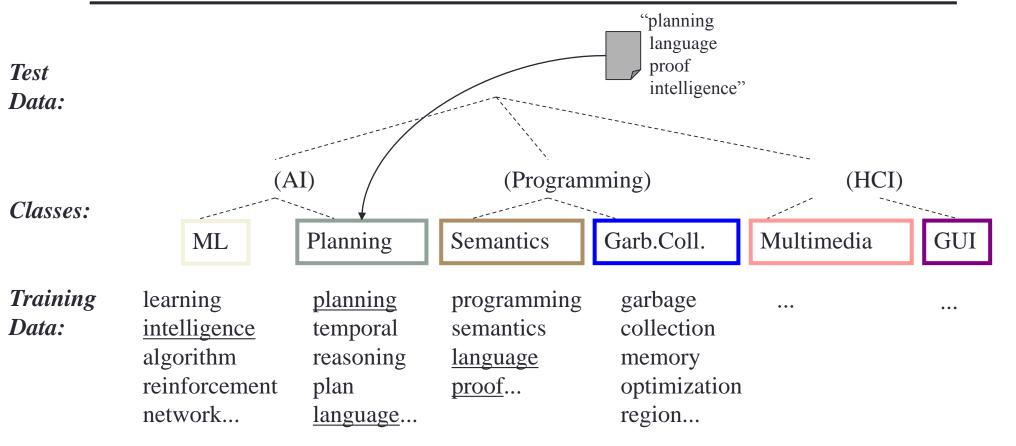
- A description of an instance, x∈X, where X is the instance language or instance space.
 - Issue: how to represent text documents.
- A fixed set of categories:

$$C = \{c_1, c_2, ..., c_n\}$$

Determine:

- The category of x: $c(x) \in C$, where c(x) is a categorization function whose domain is X and whose range is C.
 - We want to know how to build categorization functions ("classifiers").

Document Classification



(Note: in real life there is often a hierarchy, not present in the above problem statement; and you get papers on ML approaches to Garb. Coll.)

Text Categorization: examples

Assign labels to each document or Web-page:

- Labels are most often topics such as Yahoocategories
 - e.g., "finance," "sports," "news>world>asia>business"
- Labels may be genres
 - e.g., "editorials" "movie-reviews" "news"
- Labels may be opinion
 - e.g., "like", "hate", "neutral"
- Labels may be domain-specific binary
 - e.g., "interesting-to-me": "not-interesting-to-me", "spam": "not-spam", "contains adult language" :"doesn't"

Classification Methods (1)

- Manual classification
 - Used by Yahoo!, Looksmart, about.com, ODP, Medline
 - Very accurate when job is done by experts
 - Consistent when the problem size and team is small
 - Difficult and expensive to scale

Classification Methods (2)

- Automatic document classification
 - Hand-coded rule-based systems
 - One technique used by CS dept's spam filter, Reuters, CIA, Verity, ...
 - E.g., assign category if document contains a given boolean combination of words
 - Standing queries: Commercial systems have complex query languages (everything in IR query languages + accumulators)
 - Accuracy is often very high if a rule has been carefully refined over time by a subject expert
 - Building and maintaining these rule bases is expensive

Classification Methods (3)

- Supervised learning of a document-label assignment function
 - Many systems partly rely on machine learning (Autonomy, MSN, Verity, Enkata, Yahoo!, ...)
 - k-Nearest Neighbors (simple, powerful)
 - Naive Bayes (simple, common method)
 - Support-vector machines (new, more powerful)
 - ... plus many other methods
 - No free lunch: requires hand-classified training data
 - But data can be built up (and refined) by amateurs
- Note that many commercial systems use a mixture of methods

Bayesian Methods

- Learning and classification methods based on probability theory.
- Bayes theorem plays a critical role in probabilistic learning and classification.
- Build a generative model that approximates how data is produced
- Uses prior probability of each category given no information about an item.
- Categorization produces a posterior probability distribution over the possible categories given a description of an item.

Bayes' Rule

$$P(C, X) = P(C | X)P(X) = P(X | C)P(C)$$

$$P(C \mid X) = \frac{P(X \mid C)P(C)}{P(X)}$$

Maximum a posteriori Hypothesis

$$h_{MAP} \equiv \underset{h \in H}{\operatorname{argmax}} P(h \mid D)$$

$$= \underset{h \in H}{\operatorname{argmax}} \frac{P(D \mid h)P(h)}{P(D)}$$

$$= \underset{h \in H}{\operatorname{argmax}} P(D \mid h) P(h)$$

As *P(D)* is constant

Maximum likelihood Hypothesis

If all hypotheses are a priori equally likely, we only need to consider the P(D/h) term:

$$h_{ML} \equiv \underset{h \in H}{\operatorname{argmax}} P(D \mid h)$$

Naive Bayes Classifiers

Task: Classify a new instance D based on a tuple of attribute values $D = \langle x_1, x_2, ..., x_n \rangle$ into one of the classes $c_j \in C$

$$c_{MAP} = \underset{c_{j} \in C}{\operatorname{argmax}} \ P(c_{j} \mid x_{1}, x_{2}, \dots, x_{n})$$

$$= \underset{c_{j} \in C}{\operatorname{argmax}} \frac{P(x_{1}, x_{2}, \dots, x_{n} \mid c_{j}) P(c_{j})}{P(x_{1}, x_{2}, \dots, x_{n})}$$

$$= \underset{c_{j} \in C}{\operatorname{argmax}} \ P(x_{1}, x_{2}, \dots, x_{n} \mid c_{j}) P(c_{j})$$

$$= \underset{c_{j} \in C}{\operatorname{argmax}} \ P(x_{1}, x_{2}, \dots, x_{n} \mid c_{j}) P(c_{j})$$

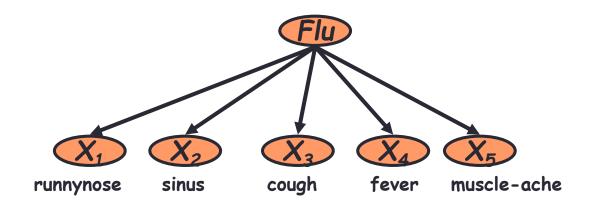
Naïve Bayes Classifier: Naïve Bayes Assumption

- $P(c_j)$
 - Can be estimated from the frequency of classes in the training examples.
- $P(x_1, x_2, ..., x_n/c_j)$
 - O(|X|ⁿ•|C|) parameters
 - Could only be estimated if a very, very large number of training examples was available.

Naïve Bayes Conditional Independence Assumption:

Assume that the probability of observing the conjunction of attributes is equal to the product of the individual probabilities $P(x_i|c_i)$.

The Naïve Bayes Classifier

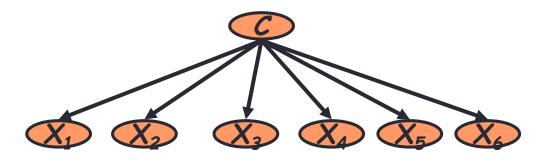


 Conditional Independence Assumption: features detect term presence and are independent of each other given the class:

$$P(X_1,...,X_5 | C) = P(X_1 | C) \cdot P(X_2 | C) \cdot ... \cdot P(X_5 | C)$$

- This model is appropriate for binary variables
 - Multivariate binomial model

Learning the Model



- First attempt: maximum likelihood estimates
 - simply use the frequencies in the data

$$\hat{P}(c_j) = \frac{N(C = c_j)}{N}$$

$$\hat{P}(x_i \mid c_j) = \frac{N(X_i = x_i, C = c_j)}{N(C = c_j)}$$

NB Bernoulli: Learning

```
TrainBernoulliNB(\mathbb{C}, \mathbb{D})
   V \leftarrow \text{ExtractVocabulary}(\mathbb{D})
2 N ← COUNTDOCS(ID)
3 for each c ∈ C
    do N_c \leftarrow \text{COUNTDOCSINCLASS}(\mathbb{D}, c)
        prior[c] \leftarrow N_c/N
        for each t \in V
        do N_{ct} \leftarrow \text{COUNTDOCSINCLASSCONTAININGTERM}(\mathbb{D}, c, t)
            condprob[t][c] \leftarrow (N_{ct}+1)/(N_c+2)
    return V, prior, condprob
```

NB Bernoulli Model: Classification

```
APPLYBERNOULLINB(C, V, prior, condprob, d)

1 V_d \leftarrow \text{EXTRACTTERMSFROMDOC}(V, d)

2 for each c \in \mathbb{C}

3 do score[c] \leftarrow \log prior[c]

4 for each t \in V

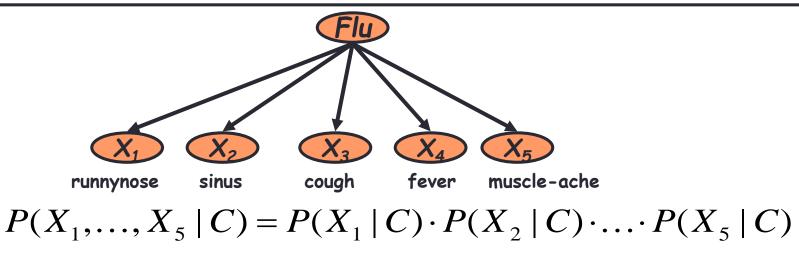
5 do if t \in V_d

6 then score[c] += \log condprob[t][c]

7 else score[c] += \log(1 - condprob[t][c])

8 return arg \max_{c \in \mathbb{C}} score[c]
```

Problem with Max Likelihood



 What if we have seen no training cases where patient had no flu and muscle aches?

$$\hat{P}(X_5 = t \mid C = nf) = \frac{N(X_5 = t, C = nf)}{N(C = nf)} = 0$$

 Zero probabilities cannot be conditioned away, no matter the other evidence!

$$\ell = \arg\max_{c} \hat{P}(c) \prod_{i} \hat{P}(x_{i} \mid c)$$

Smoothing

- Laplace smoothing
 - every feature has an a priori probability p,
 - It is assumed that it has been observed in a number of m virtual examples.

$$P(x_{j} \mid c_{i}) = \frac{n_{ij} + mp}{n_{i} + m}$$

- Usually
 - A uniform distribution on all words is assumed so that p = 1/|V| and m = |V|
 - It is equivalent to observing every word in the dictionary once for each category.

Smoothing to Avoid Overfitting

$$\hat{P}(x_i \mid c_j) = \frac{N(X_i = x_i, C = c_j) + 1}{N(C = c_j) + k}$$

of diff. values of X_i

Somewhat more subtle version

k expresses the different data bins

overall fraction in data where $X_i = x_{i,k}$

$$\hat{P}(x_{i,k} \mid c_j) = \frac{N(X_i = x_{i,k}, C = c_j) + mp_{i,k}}{N(C = c_j) + m}$$

extent of "smoothing", numb. of bins

Stochastic Language Models

 Models probability of generating strings (each word in turn) in the language (commonly all strings over ∑). E.g., unigram model

Model M

0.2	the	the	man	likes	the	woman	
0.1	a	———	——		——	WOIIIaii	
0.01	man	0.2	0.01	0.02	0.2	0.01	
0.01	woman						
0.03	said	multiply					
0.02	likes	$P(s \mid M) = 0.00000008$					

. . .

Stochastic Language Models

Model probability of generating any string

Model M1

0.2 the

0.01 class

0.0001 sayst

0.0001 pleaseth

0.0001 yon

0.0005 maiden

0.01 woman

Model M2

0.2 the

0.0001 class

0.03 sayst

0.02 pleaseth

0.1 yon

0.01 maiden

0.0001 woman

the	class	pleaseth	yon	maiden
0.2	0.01	0.0001	0.0001	0.0005
0.2	0.0001	0.02	0.1	0.01

Unigram and higher-order models

$$P(\bullet \circ \bullet \bullet)$$

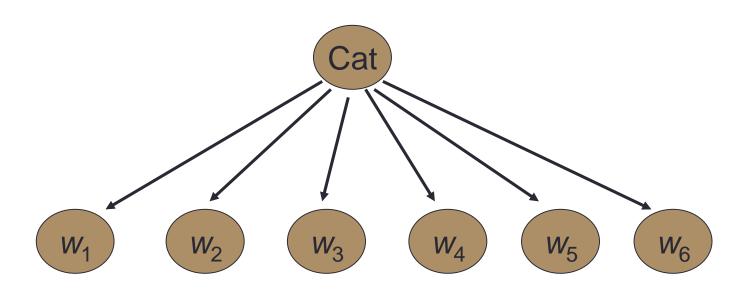
$$= P(\bullet)P(\circ | \bullet) P(\bullet | \bullet \circ)P(\bullet | \bullet \bullet)$$
• Unigram Language Models
$$P(\bullet)P(\bullet)P(\bullet)P(\bullet)$$
Easy.
Effective!

Bigram (generally, n-gram) Language Models

$$\mathbf{P}(\bullet) \mathbf{P}(\bullet|\bullet) \mathbf{P}(\bullet|\bullet) \mathbf{P}(\bullet|\bullet)$$

- Other Language Models
 - Grammar-based models (PCFGs), etc.
 - Probably not the first thing to try in IR

Naïve Bayes via a class conditional language model = multinomial NB



 Effectively, the probability of each class is done as a classspecific unigram language model

Using Multinomial Naive Bayes Classifiers to Classify Text: Basic method

Attributes are text positions, values are words.

$$c_{NB} = \underset{c_{j} \in C}{\operatorname{argmax}} P(c_{j}) \prod_{i} P(x_{i} | c_{j})$$

$$= \underset{c_{j} \in C}{\operatorname{argmax}} P(c_{j}) P(x_{1} = \text{"our"} | c_{j}) \cdots P(x_{n} = \text{"text"} | c_{j})$$

- Still too many possibilities
- Assume that classification is independent of the positions of the words
 - Use same parameters for each position
 - Result is bag of words model (over tokens not types)

Multinomial Naïve Bayes: Learning

- From training corpus, extract Vocabulary
- Calculate required $P(c_i)$ and $P(x_k / c_i)$ terms
 - For each c_i in C do
 - $docs_j \leftarrow$ subset of documents for which the target class is c_j

$$P(c_j) \leftarrow \frac{|docs_j|}{|\operatorname{total} \# \operatorname{documents}|}$$

- Text_j ← single document containing all docs_j
- for each word x_k in *Vocabulary*
 - $n_k \leftarrow$ number of occurrences of x_k in $Text_i$

$$= P(x_k \mid c_j) \leftarrow \frac{n_k + \alpha}{n + \alpha \mid Vocabulary \mid}$$

Multinomial Naïve Bayes: Classifying

- positions ← all word positions in current document which contain tokens found in *Vocabulary*
- Return c_{NR} , where

$$c_{NB} = \underset{c_{j} \in C}{\operatorname{argmax}} P(c_{j}) \prod_{i \in positions} P(x_{i} \mid c_{j})$$

Naive Bayes: Time Complexity

- Training Time: $O(|D|L_d + |C||V|)$ where L_d is the average length of a document in D.
 - Assumes V and all D_i , n_i , and n_{ij} pre-computed in $O(|D|L_d)$ time during one pass through all of the data.
 - Generally just $O(|D|L_d)$ since usually $|C||V| < |D|L_d$
- Test Time: $O(|C| L_t)$ where L_t is the average length of a test document.
 - Very efficient overall, linearly proportional to the time needed to just read in all the data.

Multinomial NB: Learning Algorithm

```
TrainMultinomialNB(\mathbb{C}, \mathbb{D})
  1 V ← EXTRACTVOCABULARY(ID)
 2 N ← COUNTDOCS(ID)
 3 for each c \in \mathbb{C}
     do N_c \leftarrow \text{COUNTDOCSINCLASS}(\mathbb{D}, c)
 5
          prior[c] \leftarrow N_c/N
          text_c \leftarrow ConcatenateTextOfAllDocsInClass(\mathbb{D}, c)
  6
          for each t \in V
          do T_{ct} \leftarrow \text{COUNTTOKENSOFTERM}(text_c, t)
 8
          for each t \in V
          do condprob[t][c] \leftarrow \frac{T_{ct}+1}{\sum_{t'}(T_{-t'}+1)}
10
      return V, prior, condprob
11
```

Multinomial NB: Classification Algorithm

```
APPLYMULTINOMIALNB(\mathbb{C}, V, prior, condprob, d)

1 W \leftarrow \text{EXTRACTTOKENSFROMDOC}(V, d)

2 \textbf{for each } c \in \mathbb{C}

3 \textbf{do } score[c] \leftarrow \log prior[c]

4 \textbf{for each } t \in W

5 \textbf{do } score[c] += \log condprob[t][c]

6 \textbf{return } arg \max_{c \in \mathbb{C}} score[c]
```

Underflow Prevention

- Multiplying lots of probabilities, which are between 0 and 1 by definition, can result in floating-point underflow.
- Since log(xy) = log(x) + log(y), it is better to perform all computations by summing logs of probabilities rather than multiplying probabilities.
- Class with highest final un-normalized log probability score is still the most probable.

$$c_{NB} = \underset{c_{j} \in C}{\operatorname{argmax}} \log P(c_{j}) + \sum_{i \in positions} \log P(x_{i} \mid c_{j})$$

Note: the two models

- Model 1: Multivariate binomial
 - One feature X_w for each word in dictionary
 - $X_w = true$ in document d if w appears in d
 - Naive Bayes assumption:
 - Given the document's topic, appearance of one word in the document tells us nothing about chances that another word appears
- This is the model used in the binary independence model in classic probabilistic relevance feedback in hand-classified data (Maron in IR was a very early user of NB)

Note: the two models (2)

- Model 2: Multinomial = Class conditional unigram
 - One feature X_i for each word pos in document
 - feature's values are all words in dictionary
 - Value of X_i is the word in position i
 - Naïve Bayes assumption:
 - Given the document's topic, word in one position in the document tells us nothing about words in other positions
 - Second assumption:
 - Word appearance does not depend on position

$$P(X_i = w | c) = P(X_i = w | c)$$

for all positions *i,j*, word *w*, and class *c*

Just have one multinomial feature predicting all words

Parameter estimation

Binomial model:

$$\hat{P}(X_{w} = true \mid c_{j}) =$$

fraction of documents of topic c_j in which word w appears

Multinomial model:

$$\hat{P}(X_i = w \mid c_j) =$$

fraction of times in which word w appears across all documents of topic c_j

- Can create a mega-document for topic j by concatenating all documents in this topic
- Use frequency of w in mega-document

Classification

- Multinomial vs Multivariate binomial?
 - Multinomial is in general better
 - See results figures later

NB example

- Given: 4 documents
 - D1 (sports): China soccer
 - D2 (sports): Japan baseball
 - D3 (politics): China trade
 - D4 (politics): Japan Japan exports
- Classify:
 - D5: soccer
 - D6: Japan
- Use
 - Add-one smoothing
 - Multinomial model
 - Multivariate binomial model

NB example

p(sports)=0.5 p(politics)=0.5

```
V = {China, soccer, baseball, Japan, trade, exports}
Multivariate Binomial
p(China|sports)=1/2 (o meglio (1+1)/(2+2))
p(soccer|sports)=(1+1)/(2+2)
p(exports|sports)=(0+1)/(2+2)
p(China|politics)=(1+1)/(2+2)
p(soccer|politics)=(0+1)/(2+2)
p(exports|politics)=(1+1)/(2+2)
p(sports|D5) ca =
  p(D5|sports)p(sports) =
  (1-p(China|sports))p(soccer|sports) .... (1-p(exports|sports))=
            1/2*1/2* ... *(1-1/4)*(0.5)
p(politics|D5) ca =
  p(D5|politics)p(politics) =
  (1-p(China|politics))p(soccer|politics) .... (1-p(exports|politics))=
            1/2*1/4* ... *(1-1/2)*(0.5)
da cui p(politics|D5) < p(sports|D5), e quindi:
  D5 \in sports AND NOT D5 \in politics
```

```
Multinomial NB
Again:
V = {China, soccer, baseball, Japan, trade, exports}
p(sports)=0.5
p(politics)=0.5
p(China|sports)=(1+1)/(4+2)
p(soccer|sports)=(1+1)/(4+2)
p(exports|sports)=(0+1)/(4+2)
p(China|politics)=(1+1)/(5+2)
p(soccer|politics)=(0+1)/(5+2)
p(exports|politics)=(1+1)/(5+2)
p(sports|D5)= ca
 = p(D5|sports)p(sports)=p(soccer|sports)p(sports)=1/6
p(politics|D5)= ca
p(D5|politics)p(politics)=p(soccer|politics)p(politics)=(1/7)*(1/2)
 =1/14
da cui p(politics|D5) < p(sports|D5), e quindi:
```

D5 \in sports AND NOT D5 \in politics

An example of Naïve Bayes

- C = {allergy, cold, well}
- e_1 = sneeze; e_2 = cough; e_3 = fever
- E = {sneeze, cough, ¬fever}

Prob	Well	Cold	Allergy
$P(c_i)$	0.9	0.05	0.05
$P(\text{sneeze} c_i)$	O.I	0.9	0.9
$P(cough c_i)$	O.I	0.8	0.7
$P(fever c_i)$	0.01	0.7	0.4

An example of Naïve Bayes (cont.)

Probability	Well	Cold	Allergy
$P(c_i)$	0.9	0.05	0.05
$P(\text{sneeze} \mid c_i)$	0.1	0.9	0.9
$P(\text{cough} \mid c_i)$	0.1	0.8	0.7
P(fever $ c_i $	0.01	0.7	0.4

$$E=\{sneeze, cough, \neg fever\}$$

$$P(well \mid E) = (0.9)(0.1)(0.1)(0.99)/P(E)=0.0089/P(E)$$

 $P(cold \mid E) = (0.05)(0.9)(0.8)(0.3)/P(E)=0.01/P(E)$
 $P(allergy \mid E) = (0.05)(0.9)(0.7)(0.6)/P(E)=0.019/P(E)$

Most likely class is allergy as:

$$P(E) = 0.0089 + 0.01 + 0.019 = 0.0379$$

 $P(well \mid E) = 0.23$, $P(cold \mid E) = 0.26$, $P(allergy \mid E) = 0.50$

Feature Selection: Why?

- Text collections have a large number of features
 - 10,000 1,000,000 unique words ... and more
- Feature Selection:
 - is the process by which a large set of available features are neglected during the classification
 - Not reliable, not well estimated, not useful
- May make using a particular classifier feasible, e.g. reduce the training time
 - Some classifiers can't deal with 100,000 of features
 - Training time for some methods is quadratic or worse in the number of features
- Can improve generalization (performance)
 - Eliminates noise features+ Avoids overfitting

Feature selection: how?

Two idea:

- Hypothesis testing statistics:
 - Are we confident that the value of one categorical variable is associated with the value of another
 - Chi-square test
- Information theory:
 - How much information does the value of one categorical variable give you about the value of another
 - Mutual information
- They're similar, but χ^2 measures confidence in association, (based on available statistics), while MI measures extent of association (assuming perfect knowledge of probabilities)

χ^2 statistics (CHI)

- Pearson's chi-square is often used to assess a tests of independence.
- A test of independence assesses whether paired observations on two variables, expressed in a <u>contingency table</u>, are independent of each other – for example, whether docs in different classes differ in the observation of a given feature (i.e. word).
- Ex. of a contingency table

	Term = jaguar	Term ≠ jaguar
Class = auto	2	500
Class ≠ auto	3	9500

χ^2 statistics (CHI)

- χ² is interested in (Obs Exp)²/Exp summed over all table entries: is the observed number what you'd expect given the marginals?
- Expected Values (assuming full independence), i.e. the "theoretical frequency" for a cell, given the hypothesis of independence

$$E_{i,j} = \frac{\sum_{k=1}^{c} O_{i,k} \sum_{k=1}^{r} O_{k,j}}{N},$$

χ² Value:

$$X^{2} = \sum_{i=1}^{r} \sum_{j=1}^{c} \frac{(O_{i,j} - E_{i,j})^{2}}{E_{i,j}}.$$

χ^2 statistics (CHI)

$$E_{1,1} = \frac{1}{N} (O_{1,1}(O_{1,1} + O_{1,2}) + O_{1,2}(O_{1,1} + O_{1,2})) =$$

$$= \frac{1}{10005} (2(2+3) + 500(2+3)) = 0.25$$

$$\chi^{2}(j,a) = \sum (O-E)^{2} / E = (2-.25)^{2} / .25 + (3-4.75)^{2} / 4.75 + (500-502)^{2} / 502 + (9500-9498)^{2} / 9498 = 12.9 \ (p < .001)$$

	Term = jaguar	Term ≠ jaguar	expected: E
Class = auto	2 (0.25)	500 <i>(502)</i>	
Class ≠ auto	3 (4.75)	9500 (9498)	observed: O

- The null hypothesis is rejected with confidence .999,
- since 12.9 > 10.83 (the value for .999 confidence).

χ^2 statistic (CHI)

There is a simpler formula for $2x2 \chi^2$:

$$\chi^{2}(t,c) = \frac{N \times (AD - CB)^{2}}{(A+C) \times (B+D) \times (A+B) \times (C+D)}$$

A = #(t,c)	$C = \#(\neg t, c)$
$B = \#(t, \neg c)$	$D = \#(\neg t, \neg c)$

$$N = A + B + C + D$$

Value for complete independence of term and category?

Feature selection via Mutual Information

- In training set, choose k words which best discriminate (give most info on) the categories.
- The Mutual Information between a word w and a class c is:

$$I(w,c) = \sum_{e_w \in \{0,1\}} \sum_{e_c \in \{0,1\}} p(e_w, e_c) \log \frac{p(e_w, e_c)}{p(e_w)p(e_c)}$$

For each word w and each category c

Feature selection via Mutual Information

- In training set, choose k words which best discriminate (give most info on) the categories.
- The Mutual Information between a word w and a class c is:

$$I(W = w, C = c) = \sum_{\substack{W = w \ C = c \ W \neq w \ C \neq c}} \sum_{C = c} p(W, C) \log \frac{p(W, C)}{p(W)p(C)}$$

For each word w and each category c

Feature selection via MI (contd.)

- For each category we build a list of k most discriminating terms.
- For example (on 20 Newsgroups):
 - *sci.electronics:* circuit, voltage, amp, ground, copy, battery, electronics, cooling, ...
 - rec.autos: car, cars, engine, ford, dealer, mustang, oil, collision, autos, tires, toyota, ...
- Greedy: does not account for correlations between terms
- Why?

Feature Selection

- Mutual Information
 - Clear information-theoretic interpretation
 - May select rare uninformative terms
- Chi-square
 - Statistical foundation
 - May select very slightly informative frequent terms that are not very useful for classification
- Just use the commonest terms?
 - No particular foundation
 - In practice, this is often 90% as good

Feature selection for NB

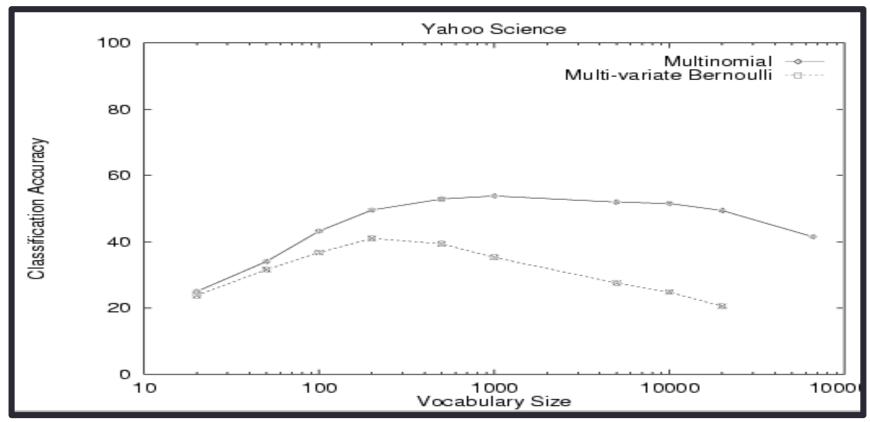
- In general feature selection is necessary for binomial NB.
- Otherwise you suffer from noise, multi-counting
- "Feature selection" really means something different for multinomial NB. It means dictionary truncation
 - The multinomial NB model only has 1 feature
- This "feature selection" normally isn't needed for multinomial NB, but may help a fraction with quantities that are badly estimated

Evaluating Categorization

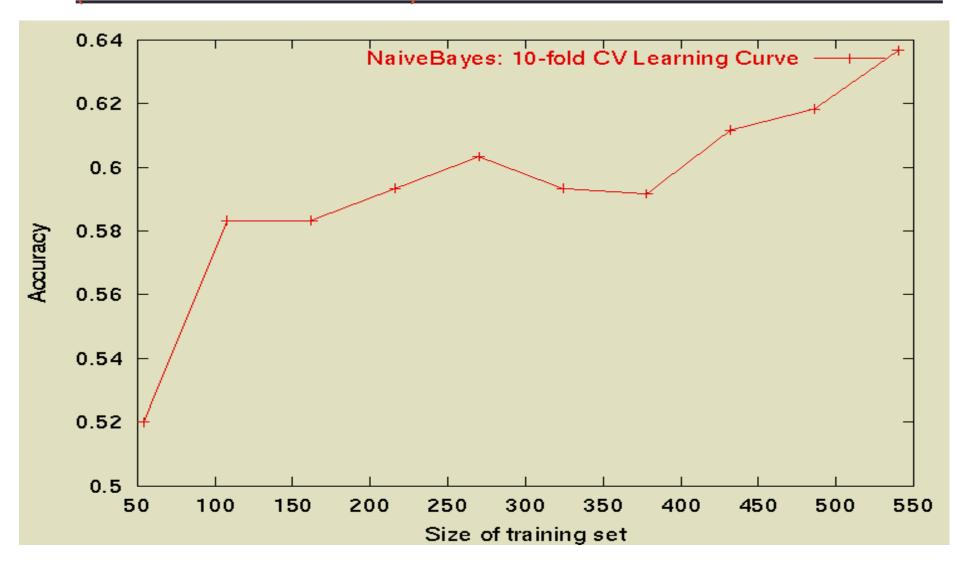
- Evaluation must be done on test data that are independent of the training data (usually a disjoint set of instances).
- Classification accuracy: c/n where n is the total number of test instances and c is the number of test instances correctly classified by the system.
- Results can vary based on sampling error due to different training and test sets.
- Average results over multiple training and test sets (splits of the overall data) for the best results.

Example: AutoYahoo!

 Classify 13,589 Yahoo! webpages in "Science" subtree into 95 different topics (hierarchy depth 2)



Sample Learning Curve (Yahoo Science Data): need more!



WebKB Experiment

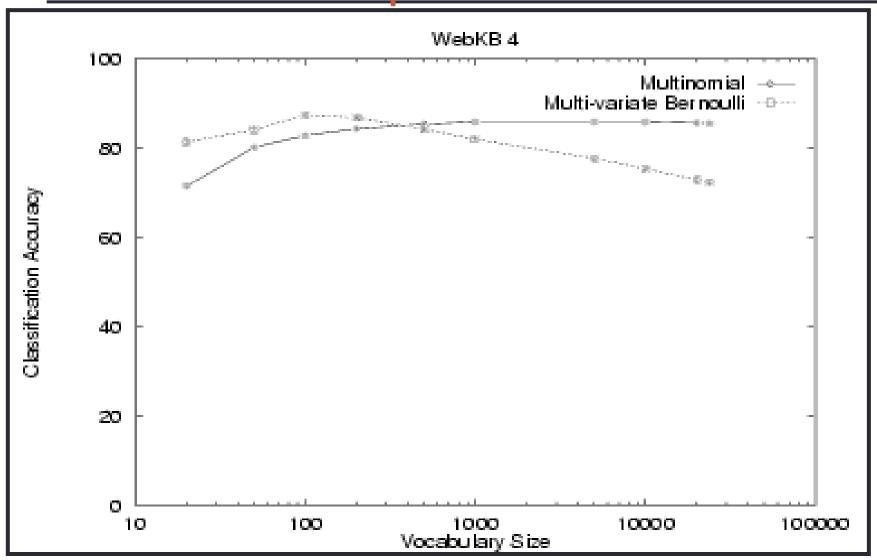
- Classify webpages from CS departments into:
 - student, faculty, course,project
- Train on ~5,000 hand-labeled web pages
 - Cornell, Washington, U.Texas, Wisconsin
- Crawl and classify a new site (CMU)

Results:



	Student	Faculty	Person	Project	Course	Departmt
Extracted	180	66	246	99	28	1
Correct	130	28	194	72	25	1
Accuracy:	72%	42%	79%	73%	89%	100%

NB Model Comparison



Faculty

associate	0.00417	
chair	0.00303	
member	0.00288	
\mathbf{ph}	0.00287	
director	0.00282	
fax	0.00279	
journal	0.00271	
recent	0.00260	
received	0.00258	
award	0.00250	

Students

Meanerm		
resume	0.00516	
advisor	0.00456	
student	0.00387	
working	0.00361	
stuff	0.00359	
links	0.00355	
homepage	0.00345	
interests	0.00332	
personal	0.00332	
favorite	0.00310	

Courses

_	
homework	0.00413
syllabus	0.00399
assignments	0.00388
exam	0.00385
grading	0.00381
midterm	0.00374
pm	0.00371
instructor	0.00370
due	0.00364
final	0.00355

Departments

departmental	0.01246
colloquia	0.01076
epartment	0.01045
seminars	0.00997
schedules	0.00879
webmaster	0.00879
events	0.00826
facilities	0.00807
eople	0.00772
postgraduate	0.00764

Research Projects

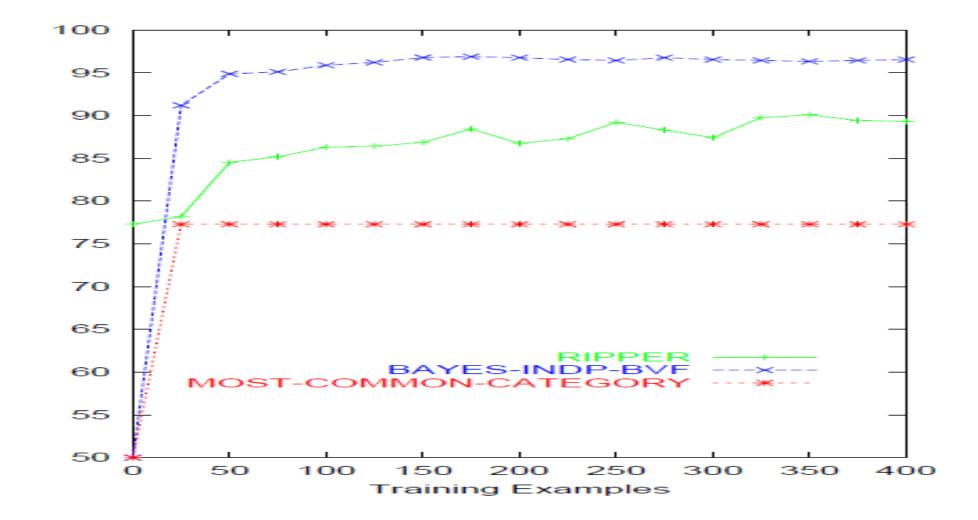
Research Projects		
investigators	0.00256	
group	0.00250	
members	0.00242	
researchers	0.00241	
laboratory	0.00238	
develop	0.00201	
related	0.00200	
агра	0.00187	
affiliated	0.00184	
project	0.00183	

Others

C cucio				
type	0.00164			
jan	0.00148			
enter	0.00145			
random	0.00142			
program	0.00136			
net	0.00128			
time	0.00128			
format	0.00124			
access	0.00117			
begin	0.00116			

Faculty		Stude	Students		Courses			
associate	0.004	17	resume	0.00516	homework	0.00413		
chair	0.0030	03	advisor	0.00456	syllabus	0.00399		
member	0.0028	38	student	0.00387	assignmen	ts 0.00388		
рh	0.0028	37	working	0.00361	exam	0.00385		
director	0.0028	32	stuff	0.00359	grading	0.00381		
fax	0.0027	79	links	0.00355	midterm	0.00374		
journal	journal 0.00271 0.00371							
recent						0.00370		
гесе	Questi insiemi di features costituiscono dei 0364							
dizionari di dominio in cui ad ogni classe								
/								
corrispondono termini specifici, come ad es.								
chair o director per i Docenti/Faculty O								
advisor per gli student: tale "conoscenza"								
emerge automaticamente dai dati annotati								
sche con la etichetta di classe								
webmaster 0.00128								
events	0	.000-			оше	0.00128		
facilities	0	.00807	arpa	0.0018	7 format	0.00124		
eople	0	.00772	affiliated	0.0018	4 access	0.00117		
postgrad	uate 0	.00764	project	0.0018	3 begin	0.00116		

Naïve Bayes on spam email



Violation of NB Assumptions

- Conditional independence
- "Positional independence"
- Examples?
 - Computer vs. science in the Technology Category
 - par vs. conditio in the Law, Politics Category
 - Box office vs. Office Box
 - Taxonomy tree vs. Tree taxonomy
 - (Dog eats vs. eating dogs) vs. (Eating vegetables vs. vegetables eat)

Naïve Bayes Posterior Probabilities

- Classification results of naïve Bayes (the class with maximum posterior probability) are usually fairly accurate.
- However, due to the inadequacy of the conditional independence assumption, the actual posterior-probability numerical estimates are not.
 - Output probabilities are generally very close to 0 or 1.

When does Naive Bayes work?

- •Sometimes NB performs well even if the Conditional Independence assumptions are badly violated.
- •Classification is about predicting the correct class label and NOT about accurately estimating probabilities.

Assume two classes c_1 and c_2 . A new case A arrives.

NB will classify A to c_1 if:

$$P(A, c_1) > P(A, c_2)$$

	$P(A,c_1)$	$P(A,c_2)$	Class of A
Actual Probability	0.1	0.01	c_1
Estimated Probability by NB	0.08	0.07	c_1

Besides the big error in estimating the probabilities the classification is still correct.

Correct estimation ⇒ accurate prediction

but NOT

accurate prediction

orrect estimation

Naive Bayes is Not So Naive

 Naïve Bayes: First and Second place in KDD-CUP 97 competition, among 16 (then) state of the art algorithms

Goal: Financial services industry direct mail response prediction model: Predict if the recipient of mail will actually respond to the advertisement – 750,000 records.

- Robust to Irrelevant Features
 - Irrelevant Features cancel each other without affecting results Instead Decision Trees can heavily suffer from this.
- Very good in domains with many <u>equally important</u> features
 Decision Trees suffer from *fragmentation* in such cases especially if little data
- A good dependable baseline for text classification (but not the best)!
- Optimal if the Independence Assumptions hold: If assumed independence is correct, then it is the Bayes Optimal Classifier for problem
- Very Fast: Learning with one pass over the data; testing linear in the number of attributes, and document collection size
- Low Storage requirements

Resources

- IIR 13
- Fabrizio Sebastiani. Machine Learning in Automated Text Categorization. ACM Computing Surveys, 34(1):1-47, 2002. (http://faure.iei.pi.cnr.it/~fabrizio/Publications/ACMCS01/ACMCS01.pdf)
- Andrew McCallum and Kamal Nigam. A Comparison of Event Models for Naive Bayes Text Classification. In AAAI/ICML-98 Workshop on Learning for Text Categorization, pp. 41-48.
- Tom Mitchell, Machine Learning. McGraw-Hill, 1997.
 - Clear simple explanation
- Yiming Yang & Xin Liu, A re-examination of text categorization methods. Proceedings of SIGIR, 1999.

<u>Summary</u>

- Un tipo di apprendimento di base è quello probabilistico dove apprendere significa
 - Descrivere il problema mediante un modello generativo che mette in relazione le variabili in input (e.g. sintomi) e quelle in output (e.g. diagnosi)
 - Determinare i corretto parametri del problema (i.e. le distribuzioni analitiche o la stima delle probabilità discrete)
- Un esempio: classificazione NB (caso discreto)
- Due sono i modelli piu' usati:
 - Multivariate Binomial (o Bernoulli) NB
 - Multinomial NB

Summary (2)

- Nella stima dei parametri in NB un ruolo centrale è svolto dalle tecniche di smoothing: a parità di modello infatti stimatori errati producono risultati insoddisfacenti
- La classificazione mediante NB è preferibile per la relativa robustezza nei casi in cui l'efficienza è fondamentale
- E' invece usato come baseline in molta sperimentazione